

# Categorical Normalizing Flows via Continuous Transformations

## Introduction

• How can we model categorical data with Normalizing Flows?



(Variational) Dequantization (Theis et al., 2016; Ho et al., 2019) - Categories ≠ quantized values

**Discrete Normalizing Flows** (Tran et al., 2019) - Difficult optimization

- Limited to permutations
- > Model categorical distributions by Normalizing Flow in continuous space

# Categorical Normalizing Flows

- Desired properties of an encoding function: No loss of information, learnable, smooth, support for higher dimension
- Variational Inference with factorized decoder:

$$p(\boldsymbol{x}) \geq \mathbb{E}_{\boldsymbol{z} \sim q(\cdot | \boldsymbol{x})} \left[ \frac{\prod_{i} p(x_i | \boldsymbol{z}_i)}{q(\boldsymbol{z} | \boldsymbol{x})} p(\boldsymbol{z}) \right]$$

- All model complexity in flow, variational inference only used for encoding
- Best encoding function: simple mixture model with exact decoder



#### Experiments – Language modeling

• Considerable better than joint decoder models (LatentNF, Ziegler et al., 2019), especially for complex datasets



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#### Experiments – Molecule generation

- Molecules: nodes are atoms, edges are bonds
- SoTA for flows without manually encoded rules
- Most common failure case: generating two unconnected valid graphs.

Method	Valid	Unique	Novel	Parallel	Manual
JT-VAE	100%	100%	100%	X	$\checkmark$
GraphAF	68%	99.10%	100%	X	X
R-VAE	34.9%	100%	-	$\checkmark$	X
GraphNVP	42.60%	94.80%	100%	$\checkmark$	X
GraphCNF	83.41%	99.99%	100%	$\checkmark$	X
+ Sub-graphs	96.35%	99.98%	99.98%	$\checkmark$	X



Paper and code



Given a graph G = (V, E):  $z_1^{(V)} = f_1\left(z_0^{(V)}; E, E_{attr}\right)$  $z_2^{(V)}, z_1^{(E_{attr})} = f_2\left(z_1^{(V)}, z_0^{(E_{attr})}; E\right)$  $z_3^{(V)}, z_1^{(E)} = f_3\left(z_2^{(V)}, z_0^{(E)}\right)$ 

### Experiments – Graph Coloring

- Assign color to each node, neighbors need different colors
- Tested different node ordering for GraphRNN based on heuristics
- GraphCNF competitive and faster than best GraphRNN



#### References

Jonathan Ho et al. (2019). "Flow++: Improving Flow-Based Generative Models with Variational Dequantization and Architecture Design." In: Proceedings of the 36th International Conference on Machine Learning, pages 2722–2730, Long Beach, California, USA. PMLR.

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Dustin Tran et al. (2019). "Discrete Flows: Invertible Generative Models of Discrete Data." In: Advances in Neural Information Processing Systems, pages 14692–14701.

Zachary M. Ziegler et al. (2019). "Latent Normalizing Flows for Discrete Sequences." In: Proceedings of the 36th International Conference on Machine Learning, pages 7673–7682, Long Beach, California, USA. PMLR.